

Objective

- Solve word problems involving linear inequalities by **defining variables**, **writing inequalities**, solving inequalities graphically and algebraically, and **writing answers as complete sentences in a group**.
- Success Criteria
 - Use each step to solve the word problems
- **Vocabulary:** perimeter, rectangle, width, length, inclusively, exceeds

Math Words – Write the corresponding symbol

■ Difference = $-$

■ Sum = $+$

■ Times = \times

■ Divided = \div

■ At least = \geq

■ Exceeds = $>$

■ At most = \leq

■ Inclusively =

■ Between =

■ Quantity =

$? \leq ?$
 $? < ? < ?$
 $()$

Linear Inequality Word Problems

All steps below should be followed for every problem.

- Explicitly define all variables.
- Write two equations or inequalities that model the situation.
- Solve the problem with a valid method of your choice. Circle ones you used.
 - Graphically
 - Algebraically with substitution
 - Algebraically with elimination
 - Algebraically with matrices
- State the final answer in complete sentences, which explains the real world meaning of the solution.

DO NOW: YOU HAVE EVERYTHING YOU
NEED TO SOLVE THIS

AM OBJ: WP: Linear Inequalities

1. Five times an unknown number is at least 3, and 8 more than the number exceeds 2. Find all possible values for the unknown number.

X = unknown number

$$\frac{5x}{5} \geq \frac{3}{5} \quad \text{and} \quad \underset{-8}{8} + x > \underset{-8}{2}$$

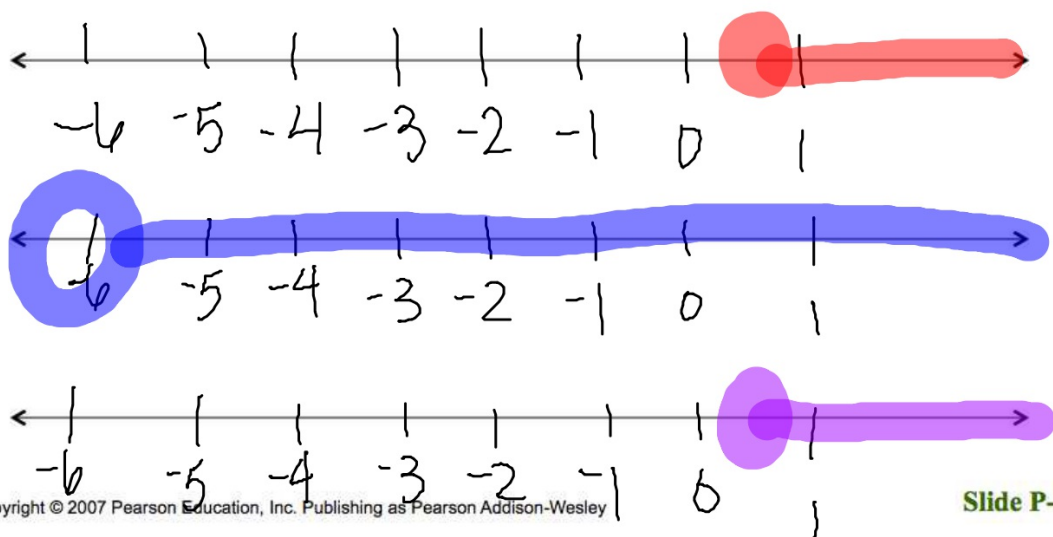
$$x \geq \frac{3}{5}$$

$$x \geq 0.6$$

$$x > -6$$

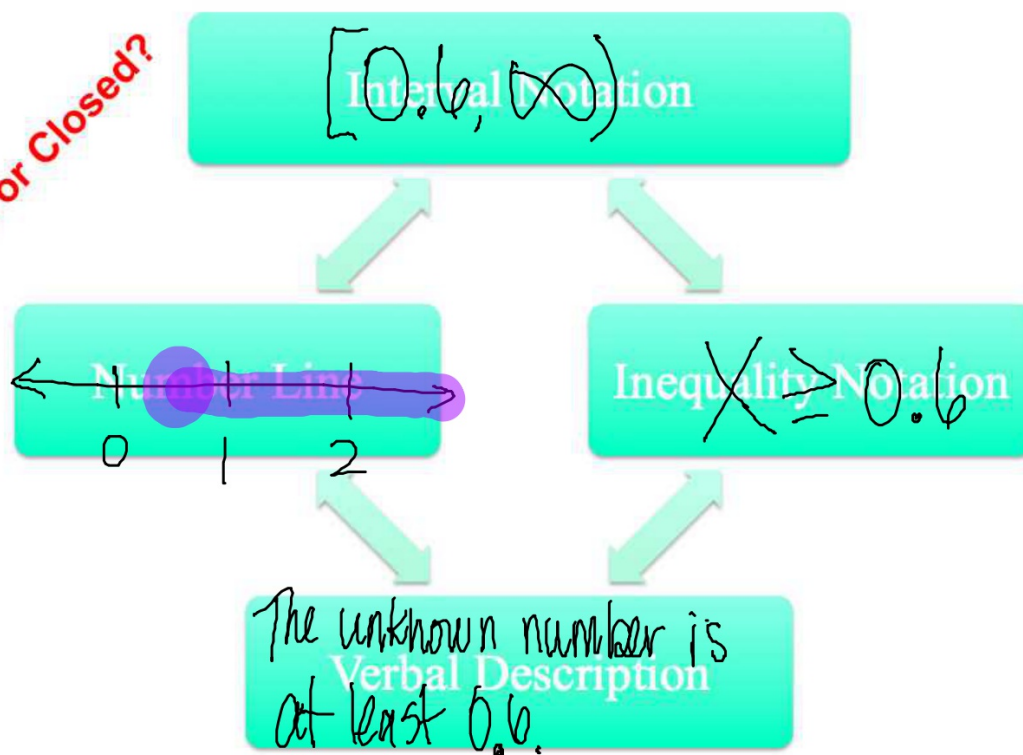
Using a graph to solve

$$x \geq 0.6 \text{ and } x > -6$$



Equivalent Representations for Intervals of Real Numbers

Open or Closed?



AM OBJ: WP: Linear Inequalities

2. The width of a rectangle is 15cm. Find all possible values for the length of the rectangle if the perimeter is at least 392 cm.

$$P = 2w + 2l \quad l = \text{length of rectangle}$$

$$2(15) + 2l \geq 392$$

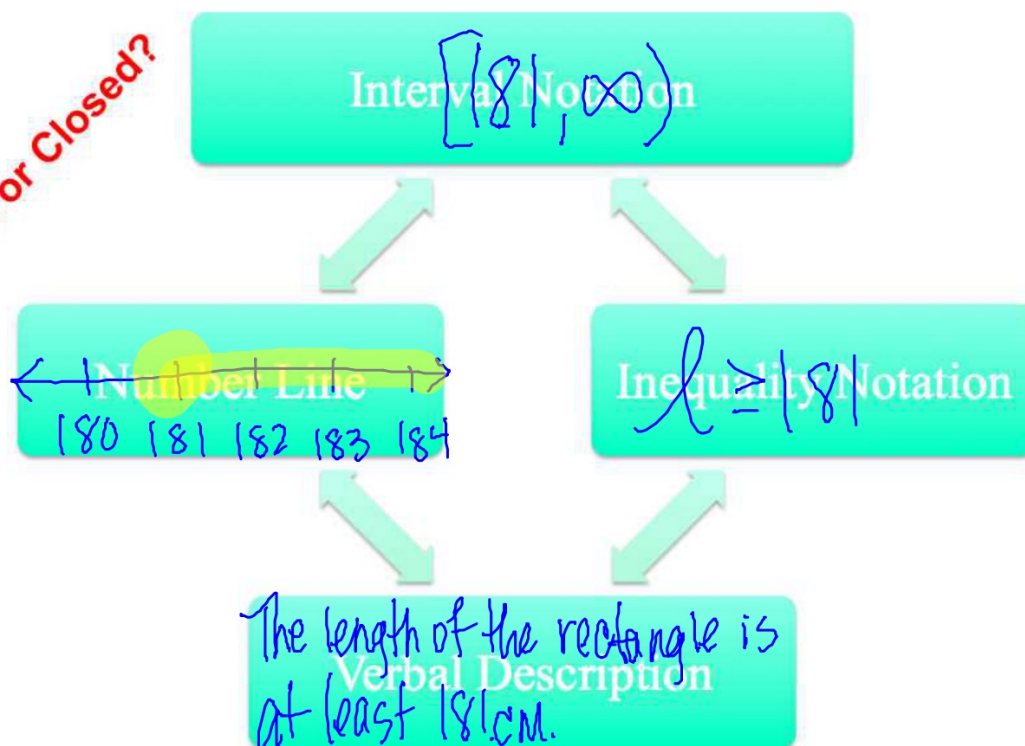
$$\begin{array}{r} 30 + 2l \geq 392 \\ -30 \quad -30 \end{array}$$

$$l \geq 181$$

$$\begin{array}{r} 2l \geq 362 \\ \underline{2} \quad \underline{2} \end{array}$$

Equivalent Representations for Intervals of Real Numbers

Open or Closed?



the set of x such that x is an element of the real #s and x is greater than or equal to $|8|$.

$\{x \mid x \in \mathbb{R}, x \geq |8|\}$ the end.

AM OBJ: WP: Linear Inequalities

$$P = 4w$$

3. The perimeter of a square is to be between 17 and 56 feet, inclusively. Find all possible values for the length of its sides.

$$\frac{17}{4} \leq \frac{4w}{4} \leq \frac{56}{4}$$

$$4.25 \leq w \leq 14$$

[A] $4.25 \leq x \leq 14$

[B] $8.5 \leq x$ and $x \leq 28$

[C] $4.25 \leq x \leq 52$

[D] $8.5 < x < 28$

$w =$ width/length
of square

Equivalent Representations for Intervals of Real Numbers

Open or Closed?

Interval Notation
 $[4.25, 14]$



Inequality Notation
 $4.25 \leq w \leq 14$

Verbal Description
The length of the sides of a square is between 4.25 and 14 inclusively.

AM OBJ: WP: Linear Inequalities

4. Five times the difference of a number and 19 is at least 155. Let x represent the number and find all possible values for the number.

$$5(x-19) \geq 155$$

[A] $x \leq 50$

[B] $x \leq 12$

$$x \geq 50$$

[C] $x \geq 12$

[D] $x \geq 50$

Equivalent Representations for Intervals of Real Numbers

Open or Closed?

