

Today's Objectives

- **Solve real-world application problems** by listening to and **analyzing** the properties of quadratic functions and **recognizing** corresponding polynomial features using **the foursquare model** as a graphic organizer.
- **Success Criteria:**
 - Apply transformations to a quadratic function
 - Rewrite quadratic in vertex form
 - Characterize quadratic functions from the verbal, algebraic, graphical, and analytical point of view.
- **Vocabulary:** quadratic, vertex, axes of symmetry, standard form, coefficients

Example Transforming the Squaring Function

Describe how to transform the graph of $f(x) = x^2$ into the graph of

$$f(x) = 2(x - 2)^2 + 3. \leftarrow \text{up 3 units}$$

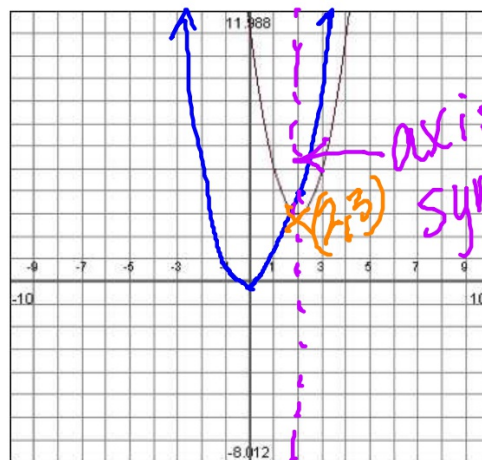
stretch
by a factor
of 2

Right
2 units

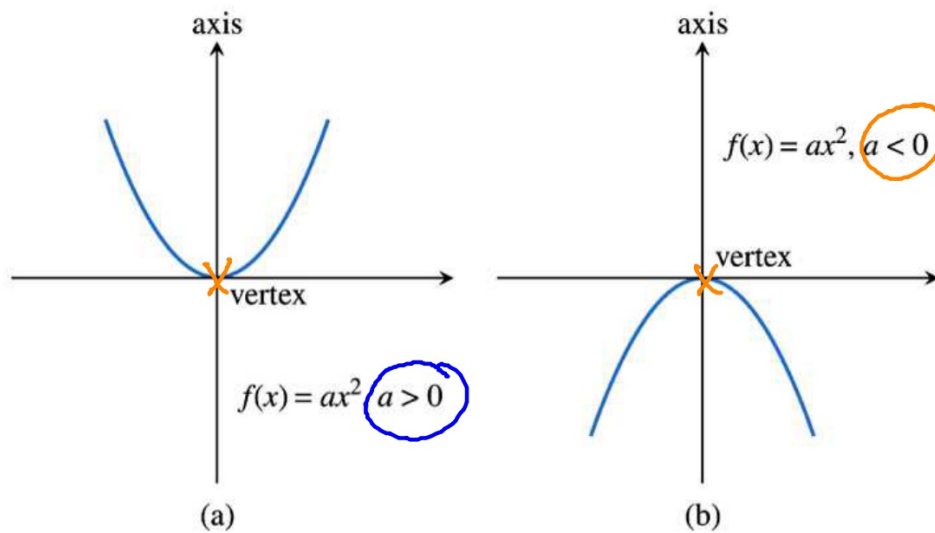
Example Transforming the Squaring Function

Describe how to transform the graph of $f(x) = x^2$ into the graph of $f(x) = 2(x - 2)^2 + 3$.

The graph of $f(x) = 2(x - 2)^2 + 3$ is obtained by vertically stretching the graph of $f(x) = x^2$ by a factor of 2 and translating the resulting graph 2 units right and 3 units up.



The Graph of $f(x) = ax^2$



Vertex Form of a Quadratic Equation

Any quadratic function $f(x) = ax^2 + bx + c$, $a \neq 0$, can be written in the vertex form

$$f(x) = a(x - h)^2 + k$$

The graph of f is a parabola with vertex (h, k) and axis $x = h$, where $h = \underline{-b/(2a)}$ and $k = \underline{c - ah^2}$.

If $a > 0$, the parabola opens upward, and if $a < 0$, it opens downward.

Example Finding the Vertex and Axis of a Quadratic Function

Use the vertex form of a quadratic function to find the vertex and axis of the graph of $f(x) = 2x^2 - 8x + 11$. Rewrite the equation in vertex form.

$$\begin{aligned} a &= 2 & b &= -8 & c &= 11 \\ h &= \frac{-b}{2a} = \frac{-(-8)}{2(2)} = \frac{8}{4} = 2 & & & & (2, 3) \\ k &= c - ah^2 = 11 - 2(2)^2 = 3 \\ f(x) &= 2(x - 2)^2 + 3 \end{aligned}$$

Example Finding the Vertex and Axis of a Quadratic Function

Use the vertex form of a quadratic function to find the vertex and axis of the graph of $f(x) = 2x^2 - 8x + 11$. Rewrite the equation in vertex form.

The standard polynomial form of f is $f(x) = 2x^2 - 8x + 11$.

So $a = 2$, $b = -8$, and $c = 11$, and the coordinates of the vertex are

$$h = -\frac{b}{2a} = \frac{8}{4} = 2 \text{ and } k = f(h) = f(2) = 2(2)^2 - 8(2) + 11 = 3.$$

The equation of the axis is $x = 2$, the vertex is $(2,3)$, and the vertex form of f is $f(x) = 2(x - 2)^2 + 3$.

Characterizing the Nature of a Quadratic Function

Fill in the following information in your 4-square graphic organizer.

Point of View

Verbal

polynomial of degree 2

Algebraic

Standard Form

$$f(x) = ax^2 + bx + c \text{ or}$$

Vertex Form

$$f(x) = a(x-h)^2 + k \quad (a \neq 0)$$

Graphical

parabola with vertex (h, k) and axis $x = h$; opens upward if $a > 0$, opens downward if $a < 0$;

initial value = y -intercept = $f(0) = c$

$$x\text{-intercepts} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

analytical

increases; decreases at different rates

AM: Solve a proportion that generates a linear or quadratic equation

3. $\frac{3y}{-18} = \frac{-6}{y-9}$

[A] $y = -12$ or $y = 3$

[B] $y = 12$ or $y = 3$

[C] $y = 12$ or $y = -3$

[D] $y = -12$ or $y = -3$

$$\cancel{(-18)}(y-9) \frac{3y}{\cancel{-18}} = \frac{-6}{\cancel{y-9}} \cancel{(-18)}(y-9)$$

$$3y^2 - 27y = 108$$
$$\quad \quad \quad -108 \quad -108$$

$$3y^2 - 27y - 108 = 0$$
$$a=3 \quad b=-27 \quad c=-108$$